

# POPULATION GROWTH

## Chapter 11

# Chapter Concepts

- 1. With abundant resources, populations can grow at geometric or exponential rates.
- 2. As resources are depleted, ....?

# Estimating Rates of An Annual Plant-ch 10

- *P. drummondii*

- $R_0$  = net reproductive rate; Avg. number of seeds produced by an individual in a population during its lifetime.

$$R_0 = \sum l_x m_x$$

$X$  = age interval in days.

$l_x = ?$

$m_x = ?$

# Estimating Rates of An Annual Plant-ch 10

- *P. drummondii*
- $R_0 = \underline{\text{net reproductive rate}}$ ;
  - ❖ Avg. number of seeds produced by an individual in a population during its lifetime.

$$R_0 = \sum l_x m_x$$

$X =$  age interval in days.

$l_x =$  % pop surviving to each age ( $x$ ).

$m_x =$  avg. number seeds produced by each individual in each age category.

## Estimating Rates of An Annual Plant-ch10

- Because *P. drummondii* has non-overlapping generations, can estimate growth rate.

- Geometric Rate of Increase ( ):

$$= N_{t+1} / N_t$$

$N_{t+1}$  = Size of population at future time.

$N_t$  = Size of population at some earlier time.

## Estimating Rates when Generations Overlap-ch10

- Common Mud Turtle (*K. subrubrum*)
  - ❖ About half turtles nest each year.
  - ❖ Avg. generation time:

$$T = \sum x l_x m_x / R_0$$

X=age in years

Per Capita Rate of Increase:

$$r = \ln R_0 / T$$

ln =base natural logarithms

# Geometric Growth

- When generations do not overlap, growth can be modeled geometrically.

$$N_t = N_0 \lambda^t$$

$N_t$  = # individuals at time  $t$ .

$N_0$  = initial # of individuals.

$\lambda$  = geometric rate of increase.

$t$  = # of time intervals or generations.

# Exponential Growth

- Continuous population growth in an unlimited env. can be modeled exponentially.

$$dN/dt = rN$$

=the change in numbers with change in time

r =the per capita rate of increase

- As population size (N) increases,
  - ❖ rate of pop.increase (dN/dt) gets larger.



# Exponential Growth

- For an exponentially growing pop., size at any time can be calculated as:

$$N_t = N_0 e^{rt}$$

- $N_t$  = # individuals at time  $t$ .
- $N_0$  = initial # of individuals.
- $e$  = base of natural logarithms.
- $r$  = per capita rate of increase.
- $t$  = number of time intervals.

- Ex. Pollen records (Bennett 1983 )
  - growth of postglacial pine pop in Britain.
  - assump: the rate of pollen deposition is prop to the size of tree pop around a lake

- Ex. Collared dove
  - ❖ Expand into W Europe, British Isles
  - ❖ 1955-72, exponential growth
  - ❖ > 1970 slow down, Env Limitation

## Chapter Concepts

- 2. As resources are depleted, population growth rate slows and eventually stops: logistic population growth.

# Logistic Population Growth

- ❖ Sigmoid (S-shaped) pop. growth curve.
- ❖ Carrying Capacity (k) is the number of individuals of a population the env. can support.
  - Finite amount of resources can only support a finite number of individuals.

- Carrying Capacity (k) is likely determined by a complex interplay among factors, e.g. food, parasitism, disease, and space....
- → Mathematical model helps..

# Logistic Population Growth

$$dN/dt = r_m N(1 - N/k)$$

- $r_m$  = max. per capita rate of increase under ideal conditions.
- $r_m$  = intrinsic rate of increase
- When  $N$  nears  $K$ , right side of the equation nears zero.
  - ❖ As pop. size increases, logistic growth rate becomes a small fraction of growth rate.
- Highest pop size when  $N=k/2$ .
- $N/k$  = environmental resistance.

# Chapter Concepts

- 3. The environment limits population growth by changing birth and death rates.
- $r = b - d$ 
  - b = birth rate
  - d = death rate



# Limits to Population Growth

- Environment limits population growth by altering birth and death rates.
  - ❖ **Density-dependent factors:**
    - Disease, Resource Competition
  - ❖ **Density-independent factors:**
    - Natural Disasters

# Galapagos Finch Population Growth

- *Boag and Grant* - *Geospiza fortis* was numerically dominant finch (1,200).
- Highly variable rainfall at Galapagos Is.  
→ pop fluctuated greatly

- After drought of 1977, pop. fell to 300.
  - Food plants failed to produce seed crop.
  - 1983 – 10x normal rainfall caused population to grow (1,100) due to abundance of seeds and caterpillars.

- Ex. Grant & Grant

large cactus finch on Genovesa Is, 1978-88

two droughts

# Cactus Finches and Cactus Reproduction

- *Grant and Grant* documented several ways finches utilized cacti:
  - ❖ Open flower buds in dry season to eat pollen.
  - ❖ Consume nectar and pollen from mature flowers.
  - ❖ Eat seed coating (aril).
  - ❖ Eat seeds
  - ❖ Eat insects from rotting cactus pads.

# Cactus Finches and Cactus Reproduction

- Finches tend to destroy stigmas, thus flowers cannot be fertilized.
  - ❖ Wet season activity may reduce seeds available to finches during the dry season.
  - ❖ *Opuntia helleri* main source for cactus finches
    - Negatively impacted by El Nino (1983).
      - Stigma snapping delayed recovery.
        - Interplay of biotic and abiotic factors.

## Chapter Concepts

- 4. On avg., small organisms have higher ( $r$ ) and more variable pops. – while large organisms have lower ( $r$ ) and less variable pops.

## Intrinsic Rates of Increase

- On average, small organisms have higher rates of per capita increase and more variable populations than large organisms.



## Pop. Growth by Small Marine Invertebrates

- Populations of marine pelagic tunicate (*Thalia democratica*) grow at exponential rates in response to phytoplankton plumes.
  - ❖ Numerical response can increase pop. size dramatically due to extremely high reproductive rates.

## Growth of A Whale Population

- Pacific Gray Whale (*Eschrichtius robustus*) divided into Western and Eastern Pacific subpopulations.
- **Rice and Wolman** estimated avg. annual mortality rate of .089 and calculated annual birth rate of 0.13. (from life table)
  - ❖  $0.13 - .089 = .041$ 
    - Gray Whale pop. Growing at 4.1% per yr.

# Growth of A Whale Population

- *Reilly et.al.* used annual migration counts from 1967-1980 to obtain 2.5% growth rate.
- Thus from 1967-1980, pattern of growth in California Gray Whale pop fit exponential model:

$$N_t = N_o e^{0.025t}$$

By 1993, pop reached 21,000=prewhaling level

# Applications to human population

- Distribution is highly clumped at large scales
- Asia
  - ❖ China & India
- Coastal area

# Population dynamics

- Vary widely from region to region, and country to country
- Exam: age distributions, birth rates & death rates of 3 countries.

- In 1997
- Lithuania,  $b=0.014$ ,  $d=0.013$ ,  $r=0.001$
- Hungary,  $b=0.011$ ,  $d=0.015$ ,  $r= -0.004$
- Rwanda,  $r=0.018$
- Predict their pop dynamic trends?

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